

# Comparison of the Expressive Power of Language-based Access Control Models

Yoshiaki Takata

Dept. of Information Systems Engineering  
Kochi University of Technology

Hiroyuki Seki

Graduate School of Information Science  
Nara Institute of Science and Technology

## Abstract

This paper compares the expressive power of five language-based access control models. We show that the expressive powers are incomparable between any pair of history-based access control, regular stack inspection and shallow history automata. Based on these results, we introduce an extension of HBAC, of which expressive power exceeds that of regular stack inspection.

**Keywords** history-based access control, stack inspection, shallow history automaton, expressive power

## 1 Introduction

To protect secure information against malicious access, it is desirable to incorporate a runtime access control mechanism in a host language. This approach is called *language-based access control*, and a few models have been proposed [1, 5, 6, 9]. A common feature of these models is that the history of execution such as method invocation and resource access is used for access control. *Stack inspection* provided in the Java virtual machine [6] is one of the best-known such control mechanisms. In stack inspection, a set of permissions is assigned statically to each method and when the control reaches a statement for checking permissions, it is examined whether or not every method on the runtime stack has the permissions specified by the statement. Stack inspection has been extended in several ways. For example, stack pattern can be specified by LTL formula in [7] and regular language in [4, 8]. Automatic verification methods for a program with stack inspection are also discussed in [4, 7, 8]. Abadi and Fournet [1] pointed out the problem of stack inspection, which completely cancels the effect of the finished method execution. They proposed a new control mechanism called *history-based access control* (HBAC). In HBAC, current permissions are modified each time a method is invoked, and they may depend on all the methods executed so far. Verification of HBAC programs is also discussed in [2, 3, 10]. Meanwhile, Schneider [9] defines *security automata*, and later Fong [5] defines *shallow history automata* as a subclass of finite-state security automata. Fong showed that the expressive powers of shallow history automata and regular

stack inspection are incomparable. However, the relations among the control models mentioned so far have not been fully clarified.

In this paper, we first define five of the existing control mechanisms in a simple and uniform framework based on control flow graph. Next, we introduce a trace equivalence relation among programs, and compare the expressive power of the five subclasses of programs. In particular, the expressive powers are incomparable between any pair of history-based access control, regular stack inspection and shallow history automata. Based on these results, we introduce an extension of HBAC, of which expressive power exceeds that of regular stack inspection.

## 2 Definitions

### 2.1 HBAC program

An HBAC program is a tuple  $\pi = (Mhd, f_0, \{G_f \mid f \in Mhd\}, PRM)$  where  $Mhd$  is a finite set of method names,  $f_0 \in Mhd$  is the main method name,  $G_f$  ( $f \in Mhd$ ) is a *control flow graph* of  $f$  defined below and  $PRM$  is a finite set of *permissions*.  $G_f$  is a directed graph  $(NO_f, TG_f, IS_f, IT_f, SP_f)$  where  $NO_f$  is a finite set of nodes,  $TG_f \subseteq NO_f \times NO_f$  is a set of *transfer edges*,  $IS_f : NO_f \rightarrow \{call_g[P_G, P_A] \mid g \in Mhd, P_G \subseteq SP_f, P_A \subseteq SP_f\} \cup \{check[P] \mid P \subseteq PRM\} \cup \{return, nop\}$  is a labeling function for nodes,  $IT_f \subseteq NO_f$  is a set of *initial nodes*, which represents the set of entry points of method  $f$ , and  $SP_f \subseteq PRM$  is a subset of permissions assigned to  $f$  before runtime (*static permissions*).  $NO_f$  is divided into four subsets by  $IS_f$  as follows.

- $IS_f(n) = call_g[P_G, P_A]$ . Node  $n$  is a *call node* that represents a call to method  $g$ . Parameters  $P_G$  and  $P_A$  are called *grant permissions* and *accept permissions*, respectively.
- $IS_f(n) = return$ . Node  $n$  is a *return node* that represents a return to the caller method.
- $IS_f(n) = check[P]$  where  $P \subseteq PRM$ . Node  $n$  is a *check node* that represents a test for the current permissions. For  $p \in PRM$ ,  $check[\{p\}]$  is abbreviated as  $check[p]$ .

- $IS_f(n) = nop$ . Node  $n$  is a *nop node* with no effect.

We write  $n \rightarrow n'$  for  $n, n' \in NO_f$  if  $\langle n, n' \rangle \in TG_f$ . Let  $NO = \bigcup_{f \in Mhd} NO_f$  and  $IS = \bigcup_{f \in Mhd} IS_f$ . For  $n \in NO$ , also let  $in(n) = \{n' \mid n' \rightarrow n\}$  and  $out(n) = \{n' \mid n \rightarrow n'\}$ .

In the figures in this paper, a dotted arrow denotes a transfer edge and a solid arrow connects between a call node and the initial node(s) of the callee method. Also, a method is surrounded by a rectangle and a set beside the rectangle denotes the static permissions of the method.

A state of  $\pi$  is a pair  $\langle n, C \rangle$  of a node  $n \in NO$  and a subset of permissions  $C \subseteq PRM$ . A *configuration* of  $\pi$  is a finite sequence of states, which is also called a *stack*. The concatenation of state sequences  $\xi_1$  and  $\xi_2$  is denoted as  $\xi_1 : \xi_2$ . The semantics of an HBAC program is defined by the transition relation  $\Rightarrow$  over the set of configurations, which is the least relation satisfying the following rules.

$$\begin{aligned} & \frac{IS(n) = call_g[P_G, P_A], n' \in IT_g}{\xi : \langle n, C \rangle \Rightarrow \xi : \langle n', C \cup P_G \cap SP_g \rangle} \\ & \frac{IS(m) = return, IS(n) = call_g[P_G, P_A], n \rightarrow n'}{\xi : \langle n, C \rangle : \langle m, C' \rangle \Rightarrow \xi : \langle n', C \cap (C' \cup P_A) \rangle} \\ & \frac{IS(n) = check[P], P \subseteq C, n \rightarrow n'}{\xi : \langle n, C \rangle \Rightarrow \xi : \langle n', C \rangle} \\ & \frac{IS(n) = nop, n \rightarrow n'}{\xi : \langle n, C \rangle \Rightarrow \xi : \langle n', C \rangle} \end{aligned}$$

The rule of *nop* for the other program subclasses in the following subsections is the same as above and will be omitted below. For a configuration  $\langle n_1, C_1 \rangle : \dots : \langle n_\ell, C_\ell \rangle$ , the stack top is  $\langle n_\ell, C_\ell \rangle$  where  $n_\ell$  and  $C_\ell$  are called the *current program point* and the *current permissions* of the configuration, respectively. The *trace set* of  $\pi$  is defined as  $\llbracket \pi \rrbracket = \{n_0 n_1 \dots n_k \mid n_0 \in IT_{f_0}, \exists C_1, \dots, C_k \subseteq PRM, \exists \xi_1, \dots, \xi_k \in (NO \times 2^{PRM})^*, \xi_i : \langle n_i, C_i \rangle \Rightarrow \xi_{i+1} : \langle n_{i+1}, C_{i+1} \rangle \text{ for } 0 \leq i < k, C_0 = SP_{f_0}, \xi_0 = \varepsilon\}$ , where  $\varepsilon$  denotes the empty sequence. For a set  $S$  of sequences, let  $\text{prefix}(S)$  denote the set of all nonempty prefixes of sequences in  $S$ .

**Example 1.** Chinese wall policy is a policy such that a user has access permission to any resources, but once the user has accessed one of the resources, (s)he loses access permission to the resources belonging to competing parties. A simplified Chinese wall policy can be represented by program  $\pi$  in Fig. 1. If the control reaches  $n_{1A}$  and  $n_{1A}$  calls  $A$ , then the current permissions lose permission  $p_B$ . Thus, if  $n_{2B}$  calls  $B$  afterward, the check at  $m_{0B}$  fails. The same situation occurs when  $B$  and  $A$  are called in this order. In fact,  $\llbracket \pi \rrbracket = \text{prefix}(\mathbf{}$

$$\begin{aligned} & n_0 n_{1A} m_{0A} m_{1A} (n_{2A} m_{0A} m_{1A} n_3 + n_{2B} m_{0B}) \\ & + n_0 n_{1B} m_{0B} m_{1B} (n_{2B} m_{0B} m_{1B} n_3 + n_{2A} m_{0A}), \end{aligned}$$

where the argument of ‘prefix’ is specified by a regular expression and + denotes the union operator.

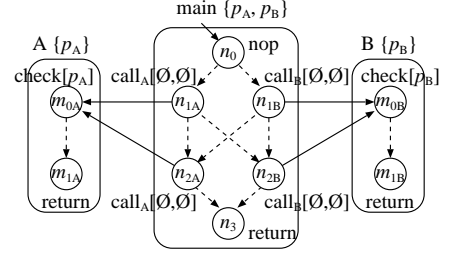


Figure 1 An HBAC program

## 2.2 JVM and R-SI programs

A program with *Java stack inspection* (abbreviated as JVM program) has a form  $\pi = (Mhd, f_0, \{G_f \mid f \in Mhd\}, PRM, PRV)$  similar to an HBAC program such that  $G_f = (NO_f, TG_f, IS_f, IT_f, SP_f)$  where each component of  $G_f$  is the same as that of an HBAC program, except that the label  $IS_f(n)$  of each call node  $n$  is simply  $call_g$  ( $g \in Mhd$ ) without  $P_G$  or  $P_A$ , and a set of privileged nodes  $PRV \subseteq NO$  is specified. The semantics of  $\pi$  is defined as follows. (The rule for *check* is the same as HBAC programs.)

$$\begin{aligned} & \frac{IS(n) = call_g, n \notin PRV, n' \in IT_g}{\xi : \langle n, C \rangle \Rightarrow \xi : \langle n', C \cap SP_g \rangle} \\ & \frac{IS(n) = call_g, n \in PRV \cap NO_f, n' \in IT_g}{\xi : \langle n, C \rangle \Rightarrow \xi : \langle n', SP_f \cap SP_g \rangle} \\ & \frac{IS(m) = return, n \rightarrow n'}{\xi : \langle n, C \rangle : \langle m, C' \rangle \Rightarrow \xi : \langle n', C \rangle} \end{aligned}$$

A *regular stack inspection* (R-SI) program  $\pi = (Mhd, f_0, \{G_f \mid f \in Mhd\})$  is introduced in [4, 8] as an extension of a JVM program where  $G_f = (NO_f, TG_f, IS_f, IT_f)$ . Its semantics is given by the following rules.

$$\begin{aligned} & \frac{IS(n) = call_g, n' \in IT_g}{\xi : n \Rightarrow \xi : n : n'} \\ & \frac{IS(m) = return, n \rightarrow n'}{\xi : n : m \Rightarrow \xi : n'} \\ & \frac{IS(n) = check[R], \xi : n \in R, n \rightarrow n'}{\xi : n \Rightarrow \xi : n'} \end{aligned}$$

where  $R \subseteq (NO)^*$  is a regular language over  $NO$ . The trace set of a JVM or R-SI program is defined in the same way as that of an HBAC program except that current permissions are missing in R-SI.

## 2.3 F-SA and SHA Programs

A *finite security automaton* (F-SA) [9] is just a deterministic finite automaton (DFA)  $M = (\Sigma, Q, q_0, \delta)$  without final states where  $\Sigma$  is a finite set of input symbols,  $Q$  is a finite set of states,  $q_0 \in Q$  is the initial state and  $\delta$  is a state transition

function, which is a partial function from  $Q \times \Sigma$  to  $Q$ . We write  $\delta(q, a) = \perp$  if  $\delta(q, a)$  is undefined. A *shallow history automaton* (SHA) [5] is an F-SA  $M = (\Sigma, Q, q_0, \delta)$  such that  $Q = 2^\Sigma$  and  $q_0 = \emptyset$  and if  $\delta(q, a) \neq \perp$  then  $\delta(q, a) = q \cup \{a\}$ .

An F-SA program is a tuple  $(Mhd, f_0, \{G_f \mid f \in Mhd\}, M)$  without permissions or check nodes where  $G_f = (NO_f, TG_f, IS_f, IT_f)$  ( $f \in Mhd$ ) and  $M = (\Sigma, Q, q_0, \delta)$  is an F-SA such that  $\Sigma = \{f, \bar{f} \mid f \in Mhd\}$ . The semantics of an F-SA program is defined as follows.

$$\frac{IS(n) = call_g, n' \in IT_g, \delta(q, g) \neq \perp}{\langle \xi : n, q \rangle \Rightarrow \langle \xi : n : n', \delta(q, g) \rangle}$$

$$\frac{IS(m) = return, m \in NO_g, n \rightarrow n', \delta(q, \bar{g}) \neq \perp}{\langle \xi : n : m, q \rangle \Rightarrow \langle \xi : n', \delta(q, \bar{g}) \rangle}$$

The trace set of an F-SA program  $\pi$  is defined as  $\llbracket \pi \rrbracket = \{n_0 n_1 \dots n_k \mid n_0 \in IT_{f_0}, \exists q_1, \dots, q_k \subseteq Q, \exists \xi_1, \dots, \xi_k \in NO^*, \langle \xi_i : n_i, q_i \rangle \Rightarrow \langle \xi_{i+1} : n_{i+1}, q_{i+1} \rangle \text{ for } 0 \leq i < k, \xi_0 = \varepsilon\}$ .

### 3 Expressive Power

A program without check nodes, permissions or privileged nodes is called a *basic program*. Let  $\alpha \in \{\text{HBAC}, \text{R-SI}, \text{JVM}, \text{F-SA}, \text{SHA}\}$ . An  $\alpha$  program  $\pi$  is an *extension* of a basic program  $\pi_0$  if  $\pi_0$  is obtained from  $\pi$  by the following operations.

- (S1) Delete each check node  $n$  (if  $\alpha = \text{HBAC}, \text{R-SI}$  or  $\text{JVM}$ ). At the same time, for any pair of  $n_1 \in in(n)$  and  $n_2 \in out(n)$ , add a transfer edge  $n_1 \rightarrow n_2$ . Moreover, if  $n \in IT_f$  for some  $f \in Mhd$ , then add every  $n_2 \in out(n)$  into  $IT_f$ .
- (S2) Delete grant permissions and accept permissions from each call node (if  $\alpha = \text{HBAC}$ ).
- (S3) Delete the designation of privileged nodes (if  $\alpha = \text{JVM}$ ).
- (S4) (Optional) For a pair of call nodes  $n_1$  and  $n_2$  in method  $f$  such that  $IS(n_1) = IS(n_2) = call_g$ ,  $in(n_1) = in(n_2)$ ,  $out(n_1) = out(n_2)$  and either  $n_1, n_2 \in IT_f$  or  $n_1, n_2 \notin IT_f$ , delete one node  $n_2$  and leave the other node  $n_1$  as it is. We call the deleted node  $n_2$  a *satellite* of  $n_1$ . This step can be repeated an arbitrary finite number of times; however, we constrain a node that has a satellite from being a satellite of another node, for consistency with later definitions.

Let  $sat(n) = \{n' \mid n' = n \text{ or } n' \text{ is a satellite of } n\}$ .

Satellite nodes can be used with check nodes for making grant permissions and accept permissions (resp. designation as a privileged node) depend on the current permissions in an HBAC (resp. JVM) program, as shown in Fig. 2. An R-SI program can contain the same structure as Fig. 2 except that the label of each check node  $m_i$  ( $1 \leq m \leq 3$ ) is  $IS(m_i) = check[R_i]$  for some regular language  $R_i$ . In this case, if  $n_i \in sat(n_1)$  is in the stack, then the prefix of the stack

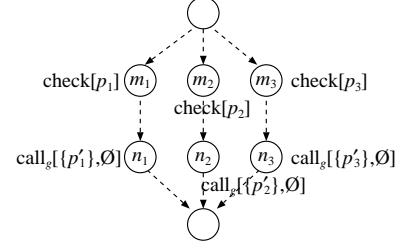


Figure 2 A call node  $n_1$  and its satellites  $n_2$  and  $n_3$

from the stack bottom to  $n_i$  matches  $R_i$ . However, the fact that a prefix of the stack matches  $R_i$  can be checked in other check nodes without using satellite nodes, and thus satellite nodes are useless in R-SI programs. On the other hand, without check nodes, satellite nodes are meaningless because  $in(n_1) = in(n_2)$  and  $out(n_1) = out(n_2)$  for a call node  $n_1$  and its satellite  $n_2$ , i.e., wherever  $n_1$  appears in an execution sequence,  $n_2$  can also appear regardless of context. Hence satellite nodes are meaningless in program models without check nodes, such as F-SA and SHA.

Let  $nc$  be a homomorphism over the set of nodes defined by  $nc(n) = n'$  for a satellite node  $n$  of  $n'$ ,  $nc(n) = n$  for a return or call node  $n$  that is not a satellite of another node, and  $nc(n) = \varepsilon$  for a check or nop node  $n$ . For two programs  $\pi_1$  and  $\pi_2$ , we say that  $\pi_1$  is *trace equivalent* to  $\pi_2$  if they are extensions of a single basic program  $\pi_0$  and  $nc(\llbracket \pi_1 \rrbracket) = nc(\llbracket \pi_2 \rrbracket)$ .

Let us denote the class of  $\alpha$  programs by  $\alpha$ . For classes of programs  $\alpha$  and  $\beta$ , we write  $\alpha \leq \beta$  if for an arbitrary  $\alpha$  program  $\pi_1$  there is a  $\beta$  program  $\pi_2$  trace equivalent to  $\pi_1$  (we say that  $\pi_1$  can be simulated by  $\pi_2$ ). If  $\alpha \leq \beta$ , we also say that  $\alpha$  can be simulated by  $\beta$ .  $\leq$  is reflexive and transitive. We write  $\alpha \not\leq \beta$  if  $\alpha \leq \beta$  does not hold. By definition,  $\text{SHA} \leq \text{F-SA}$ . It is known that  $\text{JVM} \leq \text{R-SI}$  [8],  $\text{R-SI} \not\leq \text{SHA}$ ,  $\text{SHA} \not\leq \text{R-SI}$  [5] and  $\text{JVM} \leq \text{HBAC}$  [10].

In the following theorems, we show that  $\alpha \not\leq \beta$  for any pair of program classes  $\alpha, \beta$  other than  $\text{SHA} \leq \text{F-SA}$ ,  $\text{JVM} \leq \text{R-SI}$ , and  $\text{JVM} \leq \text{HBAC}$ . Intuitively, R-SI (and JVM) cannot simulate HBAC (Theorem 1) because an R-SI program completely cancels the effect of the finished method execution. R-SI cannot simulate F-SA and SHA for the same reason. F-SA (and SHA) cannot simulate JVM (and R-SI and HBAC) (Theorem 2) because an F-SA does not consider the stack and cannot decide whether the number of calls equals the number of returns. HBAC cannot simulate SHA (and F-SA) (Theorem 5) because an HBAC program cannot simulate a program where a call to some method  $g$  enables a call to another method  $h$ .

**Theorem 1.**  $\text{HBAC} \not\leq \text{R-SI}$ .

*Proof.* Consider the HBAC program  $\pi_1$  in Fig. 3. When the control reaches  $s_0$ , the current permissions contain  $p$  if

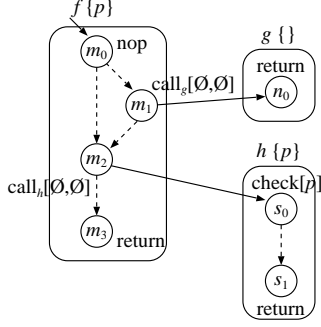


Figure 3 HBAC  $\not\leq$  R-SI

and only if  $n_0$  has never been visited. Thus the trace set of  $\pi_1$  is  $\llbracket \pi_1 \rrbracket = \text{prefix}(m_0 m_1 n_0 m_2 s_0 + m_0 m_2 s_0 s_1 m_3)$ . Suppose that there is an R-SI program  $\pi'_1$  that simulates  $\pi_1$ . Since  $nc(\llbracket \pi'_1 \rrbracket) = \text{prefix}(m_1 n_0 m_2 + m_2 s_1 m_3)$ ,  $\pi'_1$  necessarily has a check node  $s_c$  between  $m_2$  and  $s_1$ , and  $s_c$  has to abort executions that have called  $g$ . Since  $m_2$  is a call node, we can assume  $s_c = s_0$  without loss of generality. The stack at  $s_0$  after calling  $g$  has to be different from the stack at  $s_0$  when  $g$  has never been called. However, the stack at  $s_0$  must be  $m_2 s_0$ , and thus the above-mentioned check node  $s_0$  (and  $\pi'_1$ ) cannot exist.  $\square$

**Theorem 2.** JVM  $\not\leq$  F-SA.

*Proof.* The JVM program  $\pi_2$  in Fig. 4 cannot be simulated by any F-SA program. At the beginning of the program, the current permissions equal  $SP_f = \emptyset$ . However, when the privileged call node  $n_1 \in PRV$  calls  $n_0$ , the current permissions become  $SP_g = \{p\}$ . Hence when  $n_2$  calls  $s_0$ , the current permissions do not include  $p$  if and only if  $n_1$  is not in the stack, i.e.,  $n_1$  has never been visited or every call at  $n_1$  has returned. Therefore the trace set of  $\pi_2$  is  $\llbracket \pi_2 \rrbracket = \bigcup_{i \geq 1} \text{prefix}(m_0 n_0 (n_1 n_0)^{i-1} [(\varepsilon + n_2 s_0 s_1) n_3]^{i-1} (n_2 s_0 + n_3 m_1))$ .

Suppose that there exists an F-SA program  $\pi'_2$  that simulates  $\pi_2$ . The F-SA of  $\pi'_2$  must have a run (i.e. path from the initial state) for sequence  $g^i (h \bar{h} \bar{g})^{i-1} \bar{g}$  for  $i \geq 1$ <sup>1</sup> but must not have any run for  $g^j (h \bar{h} \bar{g})^{i-1} h$ . However, such a finite automaton never exists by the pumping lemma of regular languages.  $\square$

**Theorem 3.** F-SA  $\not\leq$  SHA.

*Proof.* In the program  $\pi_3$  shown in Fig. 5, calling  $h$  is permitted only when  $g$  has been called an odd number of times. If there is an SHA program  $\pi'_3$  that simulates  $\pi_3$ , then the SHA of  $\pi'_3$  must have a run for sequence  $g^{2i-1} h$  for  $i \geq 1$  but must

<sup>1</sup>By the definition of the semantics and the trace set of an F-SA program, any F-SA does not perceive the call to and the return from the initial method (e.g.  $f$  for  $\pi'_2$ ).

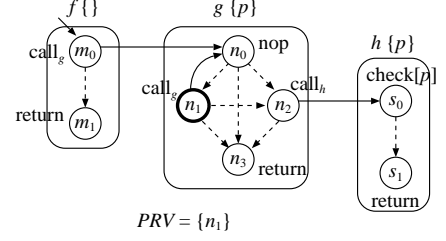


Figure 4 JVM  $\not\leq$  F-SA

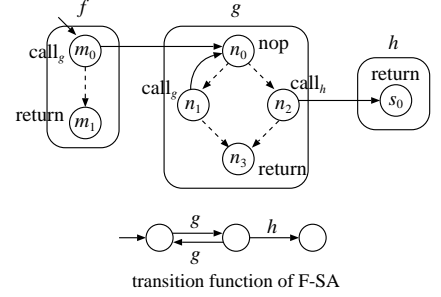


Figure 5 F-SA  $\not\leq$  SHA

not have any run for  $g^{2i} h$ . However, there is no such SHA because the state of an SHA just after reading  $g^j$  for any  $j \geq 1$  is  $\{g\}$ , and thus the SHA has a run for  $g^{2i} h$  if it has a run for  $g^{2i-1} h$ .  $\square$

Surprisingly, HBAC can simulate neither R-SI nor SHA.

**Theorem 4.** R-SI  $\not\leq$  HBAC.

*Proof.* Consider the R-SI program  $\pi_4$  in Fig. 6. This program recursively calls  $n_0$  arbitrary times, and then returns at  $n_3$  if the call at  $n_1$  was repeated an even number of times. Thus the trace set of  $\pi_4$  is  $\llbracket \pi_4 \rrbracket = \bigcup_{i \geq 1} \text{prefix}(n_0 (n_1 n_0)^{2i-2} n_2 n_3^{2i-1} + n_0 (n_1 n_0)^{2i-1} n_2)$ .

Suppose that there exists an HBAC program  $\pi'_4$  that simulates  $\pi_4$ , i.e.,  $nc(\llbracket \pi'_4 \rrbracket) = \bigcup_{i \geq 1} \text{prefix}(n_1^{2i-2} n_3^{2i-1} + n_1^{2i-1})$ . Note that in an HBAC program, the current permissions alter only at a call and return. At the beginning of  $\pi'_4$ , the current permissions equal  $SP_g$ . If the current permissions equal  $SP_g$  at  $n_1$  or  $n_1$ 's satellite in  $\pi'_4$ , then the current permissions just after the call at the node equal  $(SP_g \cup P_G) \cap SP_g = SP_g$ , where  $P_G$  is the grant permissions of the node. Thus regardless of the number of calls at a node in  $sat(n_1)$ , the current permissions remain  $SP_g$ , and thus  $\pi'_4$  cannot distinguish between even and odd numbers of calls at the nodes in  $sat(n_1)$ .  $\square$

**Theorem 5.** SHA  $\not\leq$  HBAC

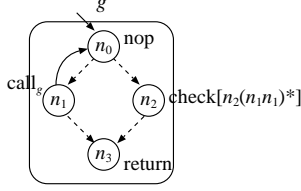


Figure 6 R-SI  $\not\leq$  HBAC

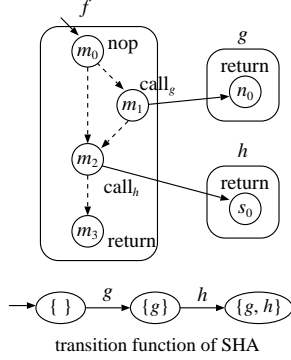


Figure 7 SHA  $\not\leq$  HBAC

*Proof.* In the SHA program  $\pi_5$  in Fig. 7, a call to  $h$  is permitted only when a call to  $g$  has occurred. Suppose that there exists an HBAC program  $\pi'_5$  that simulates  $\pi_5$ , i.e.,  $nc(\llbracket \pi'_5 \rrbracket) = \text{prefix}(m_1 n m_2 p m_3 + m_2)$ . The HBAC program  $\pi'_5$  necessarily has a check node  $s_c$  between  $m_2$  (or  $m_2$ 's satellite) and  $s_0$ , and  $s_c$  has to abort executions that have never called  $g$ . Let  $C_{02}$  be the current permissions when the control reaches a node in  $\text{sat}(m_2)$  without calling  $g$ , and let  $C_{012}$  be the current permissions when the control reaches a node in  $\text{sat}(m_2)$  after calling  $g$ . By definition,  $C_{02} = SP_f$  and  $C_{012} \subseteq SP_f$ . If the control reaches  $s_c$  and  $g$  has been called, then the current permissions become  $(C_{012} \cup P_G) \cap SP_h$ , where  $P_G$  is the grant permissions of some  $m'_2 \in \text{sat}(m_2)$ . Since  $C_{012} \subseteq C_{02}$ ,  $m'_2$  can be reached even when  $g$  has never been called. If the control reaches  $s_c$  via  $m'_2$  and  $g$  has never been called, then the current permissions become  $(C_{02} \cup P_G) \cap SP_h$ . The check node  $s_c$  must not abort the execution in the former case but must abort the execution in the latter case. However, there can be no such check node since  $C_{012} \subseteq C_{02}$ .  $\square$

## 4 An Extended Model

An HBAC program cannot remove a permission from the current permissions unless it takes the intersection of the current permissions and the static permissions of a callee

method. Thus, we extend HBAC by introducing a subset  $SET$  of  $NO$  (like  $PRV$  in a JVM program) such that if  $n \in NO_f \cap SET$  and  $IS(n) = \text{call}_g[P_G, P_A]$  in HBAC then  $n$  replaces the current permissions with  $P_G$  before taking the intersection of the current permissions and the static permissions of  $g$ . We also extend HBAC so that the initial current permissions  $C_0$  in the definition of the trace set can be an arbitrary subset of  $SP_{f_0}$  and is given as a component of an HBAC program.

The syntax and semantics of the extended model, called sHBAC, are defined as follows.

- An sHBAC program is  $\pi = (Mhd, f_0, \{G_f \mid f \in Mhd\}, PRM, SET, C_0)$ .
- The semantic rules for an sHBAC program are the rules obtained from the original rules in Section 2.1 by replacing the first rule with the following two rules.

$$\frac{IS(n) = \text{call}_g[P_G, P_A], n \notin SET, n' \in IT_g}{\xi : \langle n, C \rangle \Rightarrow \xi : \langle n', C \rangle : \langle n', (C \cup P_G) \cap SP_g \rangle}$$

$$\frac{IS(n) = \text{call}_g[P_G, P_A], n \in SET, n' \in IT_g}{\xi : \langle n, C \rangle \Rightarrow \xi : \langle n', C \rangle : \langle n', P_G \cap SP_g \rangle}$$

The definition of trace equivalence is the same as the one in Section 3 except that we add:

- (S3') Delete the designation of set nodes (nodes being in  $SET$ ) if  $\alpha = \text{sHBAC}$ .

### Theorem 6. R-SI $\leq$ sHBAC

*Proof.* Let  $\pi = (Mhd, f_0, \{G_f \mid f \in Mhd\})$  be an arbitrary R-SI program. At first, we consider a simple case in which  $\pi$  has only one check node  $n_c$ . Assume that  $IS(n_c) = \text{check}[R]$  and  $R$  is specified by a DFA  $M_R = (NO, Q, q_0, F, \delta)$ , where  $Q = \{q_0, q_1, \dots, q_k\}$  is a set of states,  $q_0 \in Q$  is the initial state,  $F \subseteq Q$  is a set of final states, and  $\delta : Q \times NO \rightarrow Q$  is a state transition function. The alphabet of  $M_R$  is the node set  $NO$  of  $\pi$ . We can construct an sHBAC program  $\pi' = (Mhd, f_0, \{G'_f \mid f \in Mhd\}, PRM, SET, C_0)$  that simulates  $\pi$  as follows. Define  $PRM = Q$ ,  $SP_f = PRM$  for all  $f \in Mhd$ , and  $C_0 = \{q_0\}$ . For each  $f \in Mhd$ , the control flow graph  $G'_f$  is the same as  $G_f$  except that each call node  $n$  is replaced with the structure shown in Fig. 8 and the check node  $n_c$  is replaced with the structure shown in Fig. 9. Define  $SET$  be the set of all call nodes in  $\pi'$ . In an execution of  $\pi'$ , the current permissions represent the state of  $M_R$  for the current stack (except the topmost node; i.e., the current permissions equal the singleton  $\{\delta(\dots \delta(\delta(q_0, m_1), m_2), \dots, m_{j-1})\}$  if the stack equals  $m_1 m_2 \dots m_{j-1} m_j$ ). The structure in Fig. 8 selects a call node  $n_i$  corresponding to the current state  $q_i$  of  $M_R$  and  $n_i$  sets the next state  $q'_i = \delta(q_i, n)$  of  $M_R$  to the current permissions. The structure in Fig. 9 blocks the execution unless the current state of  $M_R$  is a final state.

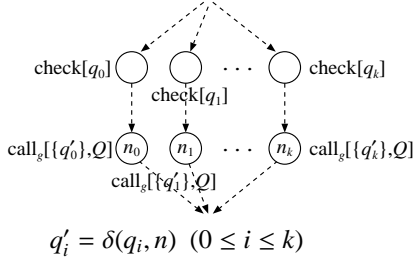


Figure 8 Structure for replacing a call node in an R-SI program

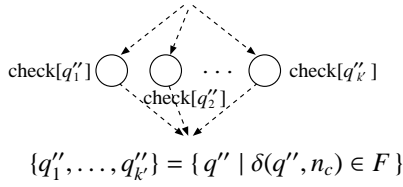


Figure 9 Structure for replacing a check node in an R-SI program

Consider the case in which  $\pi$  has more than one check nodes  $n_{c1}, \dots, n_{cm}$ . Let  $M_R$  be the product automaton of  $M_{R_1}, \dots, M_{R_m}$  where  $M_{R_i}$  ( $1 \leq i \leq m$ ) is the DFA specified for  $n_{ci}$ . Also let  $FF_i = Q_1 \times \dots \times Q_{i-1} \times F_i \times Q_{i+1} \times \dots \times Q_m$  for  $1 \leq i \leq m$  where  $Q_j$  and  $F_j$  ( $1 \leq j \leq m$ ) are the state set and the final state set of  $M_{R_j}$ , respectively. In other words,  $FF_i$  is the set of  $M_R$ 's states that contains a final state of  $M_{R_i}$  as a component. Then construct  $\pi'$  as stated above, except that when replacing each check node  $n_{ci}$ , we consider  $FF_i$  as  $F$ .  $\square$

In the sHBAC program  $\pi'$  in the proof of Theorem 6, the accept permissions of every call node in method  $f$  equal  $SP_f$ . This means that the effect of finished method execution is canceled and thus the current permissions depend only on the current stack. We call the class of such restricted sHBAC programs sH-SI. By the proof of Theorem 6,  $R\text{-SI} \leq \text{sH-SI}$ . Moreover, we can show  $\text{sH-SI} \leq R\text{-SI}$ .

**Theorem 7.**  $\text{sH-SI} \leq R\text{-SI}$

*Proof.* For a given sH-SI program  $\pi = (Mhd, f_0, \{G_f \mid f \in Mhd\}, PRM, SET, C_0)$ , consider a DFA  $M = (NO, 2^{PRM}, C_0, F, \delta)$  defined as follows. The alphabet of  $M$  is the node set  $NO$  of  $\pi$ , the state set is the power set of  $PRM$ , and the initial state is  $C_0$ . For each call node  $n$  of  $\pi$  such that  $IS(n) = call_g[P_G, P_A]$  and each subset  $C \subseteq PRM$ ,  $\delta(C, n) = (C \cup P_G) \cap SP_g$  if  $n \notin SET$  and  $\delta(C, n) = P_G \cap SP_g$  if  $n \in SET$ . For any other node  $m$  and each subset  $C \subseteq PRM$ ,  $\delta(C, m) = C$ . The state of  $M$  after reading a node sequence  $\sigma$  represents the current permissions of  $\pi$  when the stack is  $\sigma$ .

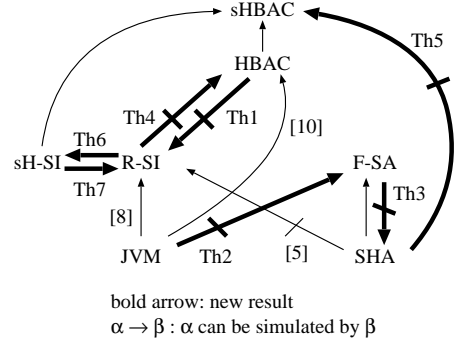


Figure 10 Comparison of the expressive power

We can construct an R-SI program  $\pi'$  that simulates  $\pi$  as follows. For each check node  $n$  such that  $IS(n) = check[P]$ , change the label to  $IS(n) = check[R]$  where the regular language  $R$  is given by a copy of  $M$  whose final state set  $F$  is  $\{C \mid P \subseteq C\}$ .  $\square$

Note that  $\text{HBAC} \leq \text{sHBAC}$  by definition.  $\text{SHA} \not\leq \text{sHBAC}$  since the proof of Theorem 5 remains valid for sHBAC.

Known results and new results are summarized in Fig. 10. For any pair of program classes  $\alpha, \beta$ , either  $\alpha \leq \beta$  or  $\alpha \not\leq \beta$  has been proved. In the figure, an arrow is omitted between program classes  $\alpha$  and  $\beta$  if  $\alpha \leq \beta$  or  $\alpha \not\leq \beta$  can be implied by other relations. For example,  $R\text{-SI} \not\leq \text{JVM}$  is implied by  $\text{JVM} \leq \text{HBAC}$  and  $R\text{-SI} \not\leq \text{HBAC}$ .

## 5 Conclusion

The expressive power of five subclasses of programs with access control was compared. In particular, the expressive powers are incomparable between any pair of history-based access control, regular stack inspection and shallow history automata. Based on these results, we introduced an extension of HBAC, of which expressive power exceeds that of regular stack inspection. It is left as a future study to clarify whether some composition of programs can simulate HBAC, for example,  $\text{HBAC} \leq \text{JVM} \times \text{SHA}$  and/or  $\text{HBAC} \leq R\text{-SI} \times \text{F-SA}$ .

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