## Computing Citation <br> Relatedness U sing Kernels

## Takahiko Ito

N ara Institute of Science and Technology

## Graph data are ubiquitous

- A huge amount of data can be represented by graphs.
- W W W , citation or social networks
- Node: web page, person
- Edge: hyperlink, citation

- We can get useful information from these types of graph data, however ...


## M otivation

- Exploring huge graphs is a difficult task
- Ex. Visualization techniques can show only a fraction of huge graphs at a time.
- Services to explore huge graphs data are desirable!


## To recommend nodes

## - Relatedness measures:

- M easures for analyzing the relationship among nodes in graphs based on graph structures.
- However, classical relatedness measures have some limitations, if they are applied to recommendation services.
- We propose to extend traditional relatedness measures based on kernel methods.


## Recommendation service for graph data

U sers select favorite nodes (root nodes) - papers / web pages
Based on links or citations around the root nodes, the service recommends other nodes that may have some relatedness to the root nodes.


## O utline

Introduce traditional relatedness measures Two problems with traditional relatedness measures
To overcome the problems, we apply two kernel methods as relatedness measures.

1. Neumann kernel [Kandola et al., 2003]
2. Regularized Laplacian kernel [Smola and Kondor, 2003]
Experiments

## Co-citation/bibliographic coupling

 "relatedness"Co-citation coupling [Small et al., 1973] defines relatedness as the number of papers jointly citing the given pair of papers

Bibliographic coupling [Kessler,1963] defines relatedness as the number of common citations made by two papers

## Computing co-citation/bibliographic

 couplingGiven adjacency matrix A of a citation graph,

- (i, j)-element of $A^{\top} A$
$\rightarrow$ Co-citation relatedness between nodes $i$ and $j$
- (i, j)-element of AA ${ }^{\top}$
$\rightarrow$ Bibliographic relatedness between nodes i and j


## Problem with classic relatedness 1

- If a pair of papers does not jointly cite or is not jointly cited by any paper, co-citation and bibliographic coupling cannot measure relatedness between the two nodes.


## $A$


bibliographic coupling $(A, B)=0$

## Problem with classical relatedness 2

- Intuition behind bibliographic coupling relatedness:

Two papers are related if they jointly make citation to one or more papers.

- But the number of other citations to the cited papers are ignored.


## Problem with classic relatedness 2:

Illustration
Which of A or C is more related to B ?


Intuition:
$C$ is more related to $B$ than $A$ is, because $A$ and $B$ only share citations to "generic" (or "popular", or "authoritative") pages (Google and Yahoo).

## N eumann kernels [Kandola et al., 2003]

- O riginal Neumann kernels compute document relatedness, but not on the basis of citations.
- They use graphs induced from the content of documents: An edge between nodes (documents) has a weight based on the number of common terms in their contents.
Definition:

$$
N K_{\beta}\left(X X^{\top}\right)=X X^{\top}+\beta\left(X X^{\top}\right)^{2}+\beta^{2}\left(X X^{\top}\right)^{3}+\ldots \quad \text { (document relatedness) }
$$

$$
N K_{\beta}\left(X^{\top} X\right)=X^{\top} X+\beta\left(X^{\top} X\right)^{2}+\beta^{2}\left(X^{\top} X\right)^{3}+\ldots \quad \text { (term relatedness) }
$$

where $X$ is a document-by-term matrix, and $\beta$ is a
"diffusion rate" parameter.

## N eumann kernels for citation analysis

N eumann kernels in this w ork

- are applied directly to citation graphs.
- i.e., use adjacency matrix A of a citation graph in place of document-by-term matrix $X$.
Definition:
$N K_{\beta}\left(A^{\top}\right)=A A^{\top}+\beta\left(A^{\top}\right)^{2}+\beta^{2}\left(A^{\top}\right)^{3}+\ldots$
$N K_{\beta}\left(A^{\top} A\right)=A^{\top} A+\beta\left(A^{\top} A\right)^{2}+\beta^{2}\left(A^{\top} A\right)^{3}+\ldots$
What do $\left(A A^{\top}\right)^{n}$ and $\left(A^{\top} A\right)^{n}$ in these series represent?


## Meaning of $\left(A^{T}\right)^{n}$

- Element $(i, j)$ of $\left(A A^{T}\right)^{n}=$ number of paths of length $n$ between nodes $i$ and $j$ in a bibliographic graph.
- Where bibliographic graph is derived from AA $^{\top}$
- Example:

Bibliographic graph


## W hy N eumann kernels does not solve problem 2

- Neumann kernels compute the weighted sum of $\left(A^{\top}\right)^{n}$ with $n=1 \sim \infty$

- At $n=1,\left(A A^{\top}\right)^{n}$ represents the bibliographic matrix As $n$ is increased...
- After $n=5$, all rows of $\left(A^{\top}\right)^{n}$ give an identical ranking $\mathrm{C}>\mathrm{D}>\mathrm{B}>\mathrm{A}$. This ranking is not relatedness among nodes but the HITS hub ranking.


## HITS [Kleinberg, 1999]

- computes "importance" of each node
- assigns two scores to each node:

Authority score :
N odes cited by many nodes receive a high authority score
Hub score:
N ode citing many authoritative nodes receive a high hub score.

## Summary of N eumann kernels

- N eumann kernels are not a relatedness measure because they bias towards importance.
Ex. Neumann kernels give a larger value to $A$ than $C$ with respect to $B$ (importance (A) > importance (C) in HITS hub score)

- We need to prevent Neumann kernels from biasing toward importance


## Solution to importance bias problem

- Change weights assigned to self-loops
- negative of the number of non-loop edges at each node
- Compute sum of weights of all paths between the nodes (unchanged from $N$ eumann kernels)
$\rightarrow$ N odes with a large number of edges (important nodes) receive a large discount


Graph induced by -L(AAT)

## Regularized Laplacian kernels

[Smola and Kondor, 2003]
Regularized Laplacian kernel matrix

$$
\operatorname{RLK}_{\beta}(S)=I+\beta(-L(S))+\beta^{2}(-L(S))^{2}+\beta^{3}(-L(S))^{3}+\ldots
$$

where

- S: symmetric matrix (such as $\mathrm{A}^{\top} \mathrm{A}$ or $\mathrm{AA}^{\top}$ )
- L(S): Laplacian [Chung, 1997] of S

$$
L(S)=D(S)-S
$$

- D(S): Diagonal matrix
- (i,i)-element represents the degree of node i in the graph induced by $S$


## Experiments

## Compare

- Regularized Laplacian kernels
with
- Co-citation coupling

D ataset:
Citation graph consisting of 2687 papers on natural language processing

## Regularized Laplacian kernel vs. co-citation coupling

Top ranked papers with respect to:
Marilyn A. W alker and Johanna D. M oore. Empirical studies in discourse. Computational Linguistics Vol. 23, No. 1, 1997

| RLK | Co-cite | Title |
| :--- | :--- | :--- |
| 1 | 1 |  |


| 1 | 1 | Empirical studies in discourse |
| :--- | :--- | :--- |
| 2 | 1 | Efct of |


| 2 | 1 | Effect of ... computer spoken natural language dialogue |
| :--- | :--- | :--- | :--- | Message Understanding Conference tests of discourse

The reliability of a dialogue structure coding scheme
Assessing agreement on classification tasks:
Attention, intentions, and the structure of discourse
Building a large annotated corpus of english: the Penn Treebank

| 8 | $\mathrm{n} / \mathrm{a}$ | A prosodic analysis of discourse segments in ... |
| :--- | :--- | :--- |


| $\mathrm{n} / \mathrm{a}$ | Centering: a framew ork for modeling the ... discourse |
| :--- | :--- | :--- |
| 9 | n |


| $\mathrm{n} / \mathrm{a}$ | Combining multiple knowledge sources for discourse |
| :--- | :--- | :--- |
| 10 |  |

## Conclusions

## Future work

- Two types of kernel methods (N eumann kernel and regularized Laplacian kernel) have applied to solve the problems in traditional relatedness measures.
- The two limitations in co-citation and bibliographic coupling relatedness can be overcome using the regularized Laplacian kernels.
- Comparison between other kernel methods and traditional relatedness measures.
- Application to collaborative filtering or relevance feedback.

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